

Recommendation Model for an After-School E-learning Mobile Application

Anaëlle Badier, Mathieu Lefort, Marie Lefevre

*Univ Lyon, UCBL, CNRS, INSA Lyon, LIRIS, UMR5205, F-69622 Villeurbanne, France
name.surname@liris.cnrs.fr*

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Abstract: In this article we present a learning resources recommendation system for an after-school educational mobile application. The goal of our system is to recommend relevant content among the learning resources available in the application to fit student needs and to encourage autonomous learning. The system is based on a graph of key notions to structure the application learning resources. We use the Item Response Theory method to evaluate the student knowledge and filter the most relevant resources to study depending on three learning strategies: revision, continuation and deepening. The resources filtered by the selected strategy, are ranked mainly based on a pedagogical score. The system has been implemented for the Mathematics subject and analysed for middle and high-school students in real-life conditions. In Fall 2022, we recorded the learning traces of 1 458 students that interacted with the system. By analysing experts opinions, logs and students feedback, we can conclude that our system is pedagogically relevant, appreciated and used by students.

1 INTRODUCTION

The rise of e-learning applications for several decades now led to new ways of learning. Students tends to learn more and more by themselves, looking for extra-class learning content. We are working with an after-school e-learning mobile application that provides courses and quizzes for all grade levels from middle school to university. This e-learning system is organized into subjects, containing chapters. Inside each chapter there are between 1 and 5 small courses and between 1 and 4 multiple-choice quizzes of 5 questions each. In this context, our goal is to recommend content suited for each student, within a platform accessible to many profiles. This application gathers students, who mostly work with the application in small working sessions (less than 5 minutes), and not regularly. Our research question is the following : **How to mobilize the learning resources of the application across different grade levels to offer relevant recommendations ?**

In the next section we present the scientific work related to our subject and highlight the particularities of our context. In a third part, we describe our contribution that proposes a recommendation system that meets the particularities presented in section 2. Then (section 4), based on experts reviews, learning traces analysis and students feedbacks, we show that the sys-

tem that was tested in the real context of use validates the relevance of our recommendation model and give us elements to improve our system. We discuss our implementation choices and results in section 5.

2 RELATED WORKS

As we are working with a mobile application, our context is quite similar to the MOOCs platforms, characterized by high attrition rates (Reich, 2014), but our learners use our app as an extra and not as their main support to learn. Thus, our application is a micro-learning tool (Nikou and Economides, 2018).

According to systematic reviews (Vaidhehi and Suchithra, 2018), recommendation systems in education are essentially based on content and on learner modeling (including hybrid strategies). (Guruge et al., 2021) listed several methods used in recommender systems, such as collaborative, content-based filtering, or data mining technics. To provide recommendations and adapt to the users, some systems are based on the concept of "Zone of Proximal Development" (ZPD) developed by (Vygotskiï and Cole, 1978). It consists on evaluating the knowledge level of a student to recommend slightly more difficult learning content, to make the students progress. (Baker et al., 2020) used a ZPD-based recommenda-

tion system and proved its positive effects on learning. This method requires to evaluate the student level. Several systems are using the Bloom’s competencies taxonomy (Bloom, 1956) to adapt to learner’s competencies. The Knowledge Tracing Models (Corbett and Anderson, 1994) are widely used to infer competencies and model the level of knowledge of a student (Vie and Kashima, 2019). These models aim to predict the outcomes of students over questions. Using statistics, the Item Based Theory (IRT) (Baker, 2001) is a method used to evaluate the latent level of competency of a given student. The use of IRT for intelligent tutoring systems have been studied by (Wauters et al., 2021).

Recommendation systems can be developed to help students to solve a precise task in one particular topic for example to learn programming languages (Branthôme, 2022). In our case, we want to use our recommendation system for different subjects, therefore we are not based on didactic. Other intelligent tutoring systems are based on online resources (Daher et al., 2018). The content is usually structured with ontological methods thanks to descriptive metadata and hyperlinks references (Nguyen et al., 2014) and can be organised in knowledge graphs (Rizun, 2019). Our system must be suitable for several subjects, but we do not have as many resources as the web-based systems and we cannot benefit from the meta-data description of learning resources (De Maio et al., 2012). However, we adapted some methods previously described as IRT that we use to evaluate the knowledge of a student but also to describe the difficulty level of our resources.

The system we present in the following section is designed to handle a voluntary, irregular and autonomous use with limited and internal resources.

3 RECOMMENDATION MODEL

Our strategy is to recommend a small list of chapters, ranked by relevancy, and to let the final choice to the student. Our system orients the learner from one chapter to another across several grade levels. The recommendation process is represented on Figure 1. Firstly, we organise our learning materials in a notions graph (section 3.1). We use IRT to select a recommendation strategy to filter our resources (section 3.2). We finally build a pedagogical score to rank the prefiltered resources and recommend the more relevant to the student (section 3.3).

3.1 Notions Graph of Ressources

Our learning resources are chapters that include multiple-choice quizzes, small courses and summary cards for each chapter called ”the Essentials”. We organize our chapters in a notions graph by tagging it with *prerequisite* and *expected* notions. We call *notion* a piece of knowledge useful to understand the current chapter. A notion is labelled as *prerequisite* if the learner must already understand part of the concept described by the notion to master the current chapter. The notion is *expected* if the chapter strategy is either to discover this notion, or to go further with more difficult questions on this notion. Thus a chapter can be tagged with the same notion as *prerequisite* and *expected* if this chapter enables the learner to acquire a deeper knowledge on this notion.

The tags were applied by the experts, *i.e.* the designers of the pedagogical resources according to the official French education program. 244 different notions have been applied on the 1 601 mathematics learning resources. These notions can be general such as *Triangle*, *Division* or more specific like *Fermat Theorem*. Our chapters are hence linked to each others through the different grade levels. An extract of this notion graph is represented on Figure 2.

3.2 Strategies Based on IRT

Because of our context, it is difficult to know the precise need of a student, so we decide to apply a recommendation strategy depending on how well students master the chapter they just finished. Three strategies are defined : *revision*, *continuation* and *deepening*.

This level of mastery is not defined by the average success score, because each quiz was created by a different teacher and they can be of varying levels of difficulty. Furthermore, the multiple-choice format makes it possible to guess the good answer by random choice. To define the student level on each chapter, we use IRT to estimate the latent learner mastery of the notions required in the chapter. IRT is not used here as it is often the case in the literature, to build computerized-adaptive tests, but we directly use the student estimated ability level θ to assign each student a level of mastery at the end of each quiz.

We use the 3 parameters version of the IRT model that includes a guessing parameter:

$$P(\theta) = c + (1 - c) \frac{1}{1 + e^{-a(\theta - b)}} \quad (1)$$

with θ the ability level, a the discrimination, b the difficulty and c the guessing parameters.

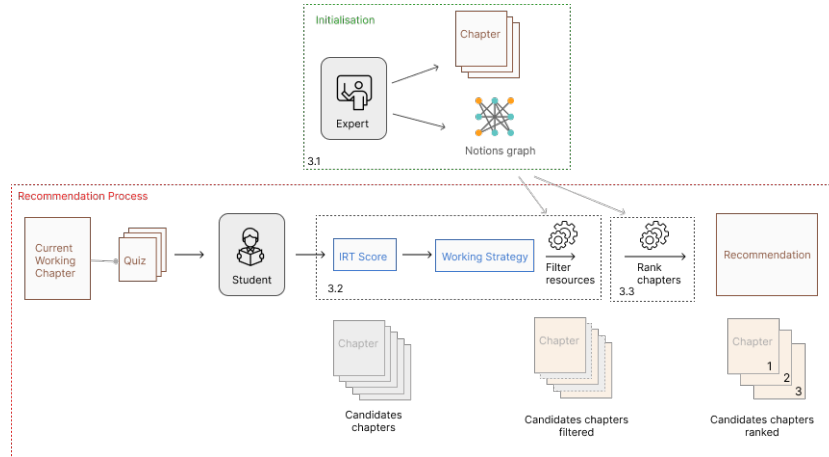


Figure 1: Recommendation workflow combining an initialisation step to build a notions graph (done only once), a filtering step based on IRT to choose among three recommendation strategies and a ranking step relying on a pedagogical score.

Firstly, we collected all the previous answers given by all students that have used the application. Using the *mirt* R package, we compute for each question the parameters a , b and c , *i.e.* the item characteristics. To compute the θ value of the quiz for a new student, we use the IRT property of local independence of the items (Baker, 2001) and apply the conditional probability formula with independent events. Given a sequence of answers correctness for a quiz (for example $seq = \{true, false, false, true, true\}$), and the items characteristics, we can compute $P(seq|\theta)$

$$P(Seq|\theta) = \prod_{i=1}^5 P_i(true/false|\theta) \quad (2)$$

with $P_i(\theta)$ computed from equation 1 with corresponding item parameters.

We can then use the iterative procedure based on the maximum likelihood described by (Baker, 2001) and assign to the learner the θ value that maximises $P(Seq|\theta)$ for a given answers sequence. From this θ we want to select a recommendation strategy for the learner at the end of a quiz. To do so, we simulate all the possible combinations for a 5-questions quiz (Q1: correct, Q2: incorrect, etc...), and for each series we got a θ score. We split this range $[\theta_{min}, \theta_{max}]$ into 3 equal ranges assigned to one different strategy. By splitting the whole range of simulated- θ in 3 groups and not using a clustering method on the students collected data, we make the strategy attribution independent of the level of the whole group of learners.

For the *revision strategy* (assigned to IRT-group low students, R on Figure 2) we focus on the *prerequisite* notions of the input chapter that are supposed not sufficiently mastered: we retain all the chapters of lower or equal grade level than the input chapter,

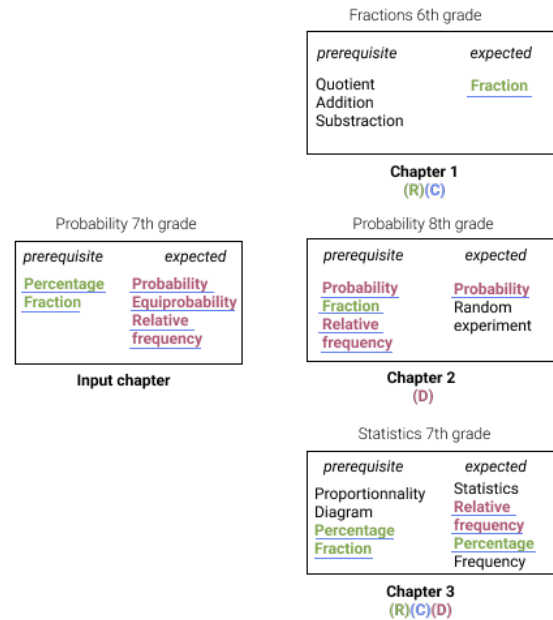


Figure 2: Example of chapters in the notion graph with corresponding recommendation strategies. Green notions are the notions in common with the prerequisite notions of the input chapter, pink notions are the notions in common with the expected notions, underlined blue notions are all notions in common with the input chapter. *R:revision*, *C:continuation*, *D:deepening*.

tagged with the input chapter prerequisite notions (in green on Figure 2). From this example, if the student ends the chapter Probability from 7th grade, we will keep the candidate chapter 1, labelled with the input chapter prerequisite *Fraction* and the candidate chapter 3 for the *Percentage* and *Fraction* notions. Chapter candidate 2 will not be prefiltered because it targets a higher grade level. The *continuation strategy* (as-

signed to IRT-group medium students, C on Figure 2) pre-filters all the chapters linked to the input chapter by a *prerequisite* or *expected* tag (both green and pink notions on Figure 2) of level equal or just one year below the input chapter. On Figure 2, chapters 1 and 3 will be selected because chapter 2 does not fit the level criterion. The *deepening strategy* (assigned to IRT-group high students, D on Figure 2) selects all the chapters of higher or equal level which notions include the input chapter *expected* notions. On the example presented on Figure 2, chapters 2 and 3 will be selected because of the notions *Probability* and *Relative frequency*. Chapter 1 has none of the input chapter expected notions, and won't pass the level criterion anyway. The choose of notions type to prefilter is discussed in section 5.

Having filtered our chapters with these 2 criteria (notion type and grade level), we finally recommend the more relevant chapters, according to the pedagogical score described on subsection 3.3.

3.3 Pedagogical Ranking

The aim of this step is to rank chapters by pedagogical relevance, to recommend resources that are related to the input chapter, *i.e* the chapter the student is working on. The pedagogical relevance score takes into account 2 components: the shared notions with the input chapter (similarity score) and the distance to the academic level of this chapter.

$$score_{peda} = score_{similarity} * (1 - penalty_{distance}) \quad (3)$$

The similarity score is calculated by taking into account the shared notions (considering prerequisite and/or expected depending on the previously selected strategy) between the available chapters and the input chapter. To do so, we use the cosine similarity method to compute the similarity between chapters notions, previously vectorized using the Term-Frequency Inverse-Document-Frequency (TF-IDF) index. This vectoring method is used to take into account the precision of the notions affixed (the more generic concepts will have less weight in the similarity index than the precise ones) and the number of notions assigned to each chapter.

The second criterion is the level grade distance between the input chapter grade and the others (Formula 4), which is an indirect indicator of the chapter difficulty. As the French national education programs are structured by cycles, the distance penalty is chosen in such a way as to penalise an "inter-cycle" distance (from 7th to 6th grade) more than an "intra-cycle" distance (from 8th to 7th grade). Considering

the input chapter grade level L_i , and a candidate chapter grade level L_c , if L_i and L_c belong to the same cycle, we apply the intra-cycle coefficient. Otherwise, we apply the inter-cycle coefficient.

$$penalty_{distance} = \frac{c * |L_c - L_i|}{D_{max} + 1} \quad (4)$$

with D_{max} the maximum distance between range levels (7 for now since the notions graph is build from 7th to 13th grade) and $c = 0.25$ if we are in intra-cycle, $c = 0.75$ elsewhere.

With the second criterion, two chapters having the same similarity score regarding the shared notions will be ranked to recommend the chapter whose grade level is the closest to the input chapter. As a second consequence, if a chapter A has a similarity score slightly lower than a chapter B, chapter A may still have a higher pedagogical score if its grade level is closest to the input chapter than chapter B grade level.

4 SYSTEM EVALUATION

4.1 Expert's Validation

The pedagogical relevance of our recommendations was surveyed by 5 mathematics teachers from different schools *via* a survey. We present to them a simulated use case: an imaginary student ends one chapter, and is assigned to a given strategy. We repeat this case for 8 chapters, for each of the 3 strategies. Thus, each expert evaluated 24 use cases, divided into 2 protocols (*i.e* 4 different chapters with the 3 strategies are presented for each protocol).

- In the first protocol, the teachers were asked to propose themselves a recommendation among the inner-app content, that was compared to the recommendation proposed by the system.
- In the second protocol, the other 4 of the 8 chapters not presented previously are presented to each expert for the 3 strategies. The teachers were asked to rate the recommendations proposed by the system on a 4-points Lickert scale between "highly irrelevant" and "perfectly suitable" and to explain their decision.

The results of the protocol 1 are shown in Figure 3. Among the 102 mathematics chapters available in the application for middle school and high-school grade levels, the expert's recommended chapters were also recommended by the system in 51.7% of the cases (31 cases out of 60). In 35% of the cases, their recommended chapters were in the top 1 for our system.

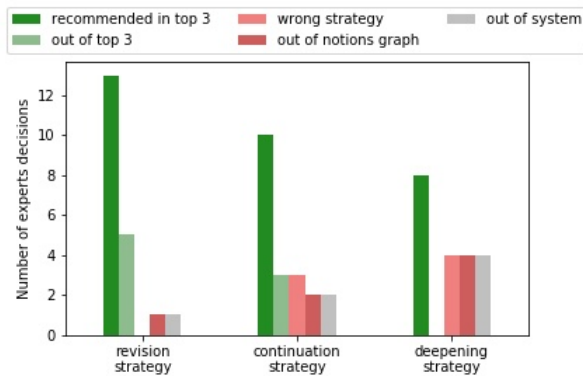


Figure 3: Results of protocol 1. Position of experts recommended chapters regarding our system, depending on the selected strategy.

8 chapters (13.3%) recommended by the experts were associated to the input chapter in the notions graph but not selected in the 3 most relevant. In 7 cases (11.7%), the experts recommendation was labeled as "wrong strategy": they recommended a lower grade-level chapter for a high-group student, or more than 1 grade-level lower chapter for a medium-group student which was not a possibility we had considered, but it was consistent with our notions graph. For other 7 cases, the recommended chapters were not in the notions graph. This limitation is discussed in section 6. 7 cases are labeled as "out of system": the experts recommended to retry the same chapter, or to go back working on a previously missed chapter instead of starting to study next grade level content, possibilities not handled by the system. The *deepening strategy* is the one on which the experts most disagreed: 2 of the experts argued that it would be too difficult for the student, or do not want the student to look ahead to the coming year by themselves.

The results of the protocol 2 are given in Figure 4. 6 cases, tagged as missing values, were not answered by 2 of the 5 experts. The experts mostly agreed with the recommendation provided by the system for the revision and continuation strategies (32/34 of rated chapters from protocol 2 were evaluated as suitable or perfectly suitable), however they would have recommended something else for the deepening strategy. 2 of the 5 experts rated all the high-group students cases recommendations at 1 and 2. They argued that it would be better to recommend for high-level students to practice more exercises from the same chapter but with more difficult questions: trying higher grade chapters would be too difficult. As the number of chapters and quizzes is limited in the application (4 quizzes of 5 questions each), this solution is unfortunately not applicable in our context. For some cases, the teacher validated the system recommendations ar-

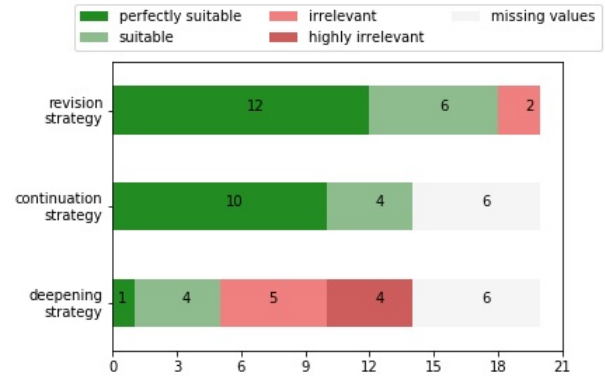


Figure 4: Results of protocol 2. Experts validation of system's recommended chapters depending on the selected strategy.

guing "The recommended chapter was in this grade level before the last educational reform, this makes sense". This validation encouraged us to recommend chapters across different level grades. These expert's comments in the survey assess that our recommendations are pedagogically relevant for most of the presented cases. However, the deepening strategy seems to be more problematic.

4.2 Real Life Experimentation

4.2.1 Implementation Design and Specificities

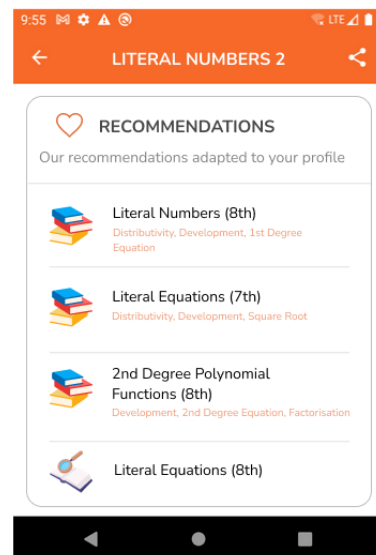


Figure 5: Recommendation interface (translated from French). The shared notions are displayed in orange. The grade level of the chapter is written in parenthesis. The system recommends 3 chapters (personalized) and one *Essential* (common to all learners).

Our recommendation model have been implemented in the mobile application for Mathematics, and was made available for all the users during 1 month since their first login to the app. The in-app recommendation interface is presented on Figure 5. We present to each student 3 recommended chapters and 1 *Essential*. The *Essential* is chosen from the student current grade level, the most similar to the current chapter according to the notions graph. The chapters recommendations are delivered from the previously described model. The scores of the chapters that were already studied by the learner, and those who were already recommended by the system are penalised by the app in order to keep novelty in the recommendations. However, it only penalises a small number of chapters and does not change the pedagogical relevance previously established.

4.2.2 Analysis of the Students Learning Traces

The system was tested in real-life conditions, that is with students working by themselves, whenever they wanted without control on their time spent using the app. We analysed the learning traces collected during 3 months of experiment: from September to November 2022. We implemented a tracking system to record interactions between the learner and the system. These data are kept for internal analysis only and deleted after 3 years according to the European privacy data protection. To analyse our results, we are using these terms:

- A *working session* is defined by all the activities recorded on the application for one student between opening and closing of the application; a student can have several working sessions for 1 day.
- A working session is a *Mathematics Active Session (MAS)* if the student started at least 1 Mathematics quiz in this working session.
- A recommendation is *chosen* if the student selects one of the recommended chapters, regardless of the time spent on this resource.

We collected the learning traces of 1 458 students that used the application for studying Mathematics during at least 1 Maths Active Session on the 3 months experiment. The number of recommendations chosen by the students, sorted by grade level is represented on Figure 6.

Among these 1 458 students, 28.9% (421 students) chose at least 1 recommendation and 11.5% (167 students) chose at least 2 recommendations. The distribution of these 1 458 students among grade levels is the following : 14.6% (213) are in 8th grade, 34.5% (503) in 9th grade, 28.6% (417) in 10th grade,

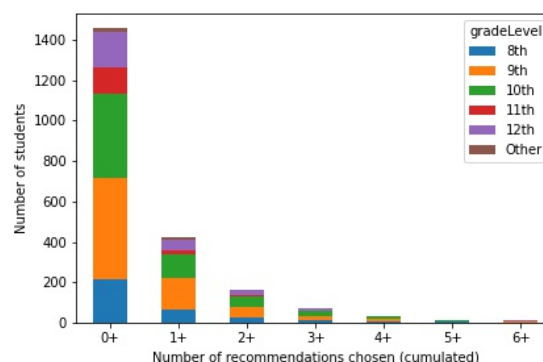


Figure 6: Distribution of students, by grade level and by number of chapters recommended chosen

8.8% (129) in 11th grade, 12.3% (179) in 12th grade and 1.2% (17) in other grades. From those who chose at least 1 recommendation (421 students), 16.4% (69) where 8th grade students, 36.3% (153) where 9th grade students and 27.6% (116) where 10th grade students. These results indicate that we manage to keep some students from different level grades using several times our recommendations. Students grade-level distribution also shows that our recommendations seems attractive for several grade levels.

4.2.3 Learner's Evaluation

We collected the student's evaluations on this recommendation system through an online survey filled by 48 students of middle school and high school grade, from different institutions at the end of the 3-months experiment. The aim of this survey was to get the user-centered indicators (Erdt et al., 2015). We wanted to evaluate their perceived usefulness, expectation and satisfaction regarding the coherence of the recommendations with the chapter studied and difficulty level. The survey contained 4 4-points Likert scale questions (Figure 7), one multi-choices question and one open-ended question.

Among the 48 students answers, 11 (24%) never seen the recommendations (*i.e* they never used the app to study Mathematics), 25 (51%) already followed a recommendation, and 12 never followed a recommendation (24%). We removed the 11 students that never viewed any recommendation from the following results analysis. Students mostly found the recommendations helpful (78.3%) and adapted (75.6%) to the chapter they were working on. Fewer think the recommendations are varied enough (72.9%), which can be explained by the low number of resources in the application. For 22 students (59.4%), these recommendations seem to be a motivating factor to spend more time working on the application. A multi-choices question asked about the perceived difficulty

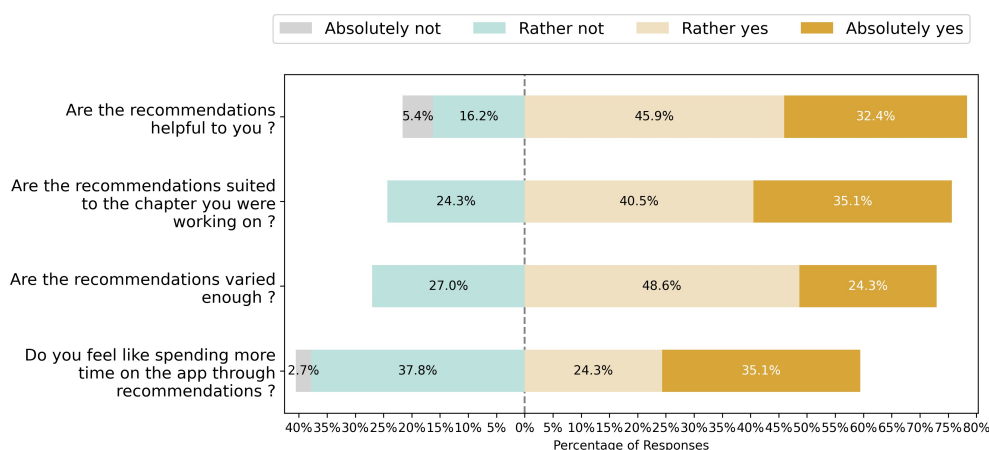


Figure 7: Likert-scale results of students survey answers.

of the recommendations: 32 found the recommended chapters difficulty appropriated, 5 too easy and 3 too difficult. An optional open-ended question asked the learner’s criteria to decide to choose a recommendation. The given answers were: the grade level displayed in parenthesis and perceived difficulty, the perceived usefulness and if the recommended chapter was already studied in class or not.

5 DISCUSSION

5.1 Implementation Choices

Notions Graph Exploration. We organized our learning resources inside a notions graph, and decided to look at all the notions in the candidates chapter for the recommendation, and to not explore the notions graph linearly. If we take the example of the input chapter on Figure 2, for a student having difficulties on this chapter, we had different choices. As the *percentage* notion is a prerequisite notion maybe not mastered enough, we could filter all the chapters of lower grade level where *percentage* is an expected notion to ensure the notion will be mastered at the end of the recommended chapter, or filter all the chapters where it is a prerequisite notion, to reinforce the mastery of this notion by using it in a different context. As these two options can be justified, we decided to consider all the chapters of lower grade having a notion in common with the prerequisite notion of the input chapter, no matter of its type. We could separately test these two hypothesis in a future work.

IRT-Driven Strategies. We choose to split the θ range in three equal groups based on the simulated results, but could have decided to restrict the deepening

strategy for the students that obtained any fixed arbitrary value or to extend the revision strategy for those whose θ is below any other arbitrary value. We chose this option as it does not add hyper-parameters to the model and allow us to gather first data to analyze, and further improve our model.

Recommendation Design. We choose to recommend only the three best chapters to the student. We wanted to let the student choose among several possibilities but within a small number of chapters to get all the recommendations displayed on the mobile screen. Moreover, with the limited number of available resources, the chapters ranked more than top-3 would be less relevant. We displayed the grade-level of the recommended chapter, which can bias the student’s decision as it has been shown in section 4.2.3. Like the displayed of the graph notions in orange, we wanted to make the system as transparent as possible.

5.2 Results Discussion

Learning Traces Analysis. We decided to label a working session as maths active (*MAS*) based on the criterion of 1 quiz started, and to assign a strategy based on quizzes results. We could have chosen others criteria such as time spent studying a Mathematics chapter, or the number of course read. We choose quizzes because in our context, our students mostly use the application to try quizzes, hence they are more representative of student’s activity on the application.

Learner’s Evaluation. Most of students declared that the recommendations were helpful and suited (section 4.2.3), however we did not observed higher following rates in learning analysis. The survey was proposed to all students having faced the recommendation system however only 48 answered. It can be explained because most students do not use the ap-

plication regularly and may not accessed the survey. That highlights the difficulty of developing a recommendation system and finding an evaluation criteria for this context.

6 CONCLUSION

We propose a recommendation system to improve navigation in a mobile application through different chapters and different grade levels. This system relies on a notions graph to link chapters, uses IRT method to assign each student a working strategy (*revision*, *continuation* or *deepening*) to filter content and build a pedagogical score to rank chapters by relevancy. It is designed for a micro-learning use and to encourage autonomous learning through the different grade levels. The system is currently implemented and used by students. Pedagogical experts approved the recommendation made for the revision and continuation strategies, and the users evaluated the system as helpful and suitable. Interviewing more experts will help to consolidate our findings and to perform some statistical analysis on the given marks. The deepening strategy seems to be more debatable mainly explained by the reluctance (of experts and students) on the use and role of an extracurricular application to discover coming years program. Concerning the experts recommendations not prefiltered by the system or those not in top three (Figure 4), we could look for a method to enhance or correct our notions graph. We assume that some students reject the recommendation because their were assigned to the wrong strategy. Analysis of students behaviour from learning traces will give the possibility to improve the system to define the best strategy for each learner. We aim to analyse deeper how learners use our recommendations, to consider students choices to improve the system knowledge, and to try our system on other subjects.

REFERENCES

- Baker, F. B. (2001). *The Basics of Item Response Theory*. ERIC Clearinghouse on Assessment and Evaluation.
- Baker, R., Ma, W., Zhao, Y., Wang, S., and Ma, Z. (2020). The results of implementing zone of proximal development on learning outcomes. In *The 13th International Conference on Educational Data Mining*.
- Bloom, B. (1956). *Taxonomy of educational objectives: The classification of educational goals*.
- Branthôme, M. (2022). *Pirates: A Serious Game Designed to Support the Transition from Block-Based to Text-Based Programming*. *Educating for a New Future: Making Sense of Technology-Enhanced Learning Adoption*, 13450:31–44.
- Corbett, A. T. and Anderson, J. R. (1994). Knowledge tracing: Modeling the acquisition of procedural knowledge. *User Modeling and User-Adapted Interaction*.
- Daher, J. B., Brun, A., and Boyer, A. (2018). Multi-source Data Mining for e-Learning. In *7th International Symposium "From Data to Models and Back (DataMod)"*.
- De Maio, C., Fenza, G., Gaeta, M., Loia, V., Orciuoli, F., and Senatore, S. (2012). RSS-based e-learning recommendations exploiting fuzzy FCA for Knowledge Modeling. *Applied Soft Computing*, 12(1):113–124.
- Erdt, M., Fernandez, A., and Rensing, C. (2015). Evaluating Recommender Systems for Technology Enhanced Learning: A Quantitative Survey. *IEEE Transactions on Learning Technologies*, 8(4):326–344.
- Guruge, D. B., Kadel, R., and Halder, S. J. (2021). The State of the Art in Methodologies of Course Recommender Systems A Review of Recent Research. *Data*, 6(2):18.
- Nguyen, C., Roussanaly, A., and Boyer, A. (2014). Learning Resource Recommendation: An Orchestration of Content-Based Filtering, Word Semantic Similarity and Page Ranking. In *9th European Conference on Technology Enhanced Learning, EC-TEL 2014*.
- Nikou, S. and Economides, A. (2018). Mobile-Based micro-Learning and Assessment: Impact on learning performance and motivation of high school students. *Journal of Computer Assisted Learning*, 34(3).
- Reich, J. (2014). MOOC Completion and Retention in the Context of Student Intent. *Educause Review*.
- Rizun, M. (2019). Knowledge Graph Application in Education: A Literature Review. *Acta Universitatis Lodzianis. Folia Oeconomica*, 3(342):7–19.
- Vaidhehi, V. and Suchithra, R. (2018). A Systematic Review of Recommender Systems in Education. *International Journal of Engineering & Technology*, 7:188.
- Vie, J.-J. and Kashima, H. (2019). Knowledge Tracing Machines: Factorization Machines for Knowledge Tracing. In *Proceedings of the AAAI Conference on Artificial Intelligence*.
- Vygotskiĭ, L. S. and Cole, M. (1978). *Mind in Society: The Development of Higher Psychological Processes*. Harvard University Press.
- Wauters, K., Desmet, P., and den Noortgate, W. V. (2021). Adaptive item-based learning environments based on the item response theory: Possibilities and challenges. *Journal of Computer Assisted Learning*, 26(6).