

# Reconstructions of Noisy Digital Contours with Maximal Primitives Based on Multi-Scale/Irregular Geometric Representation and Generalized Linear Programming



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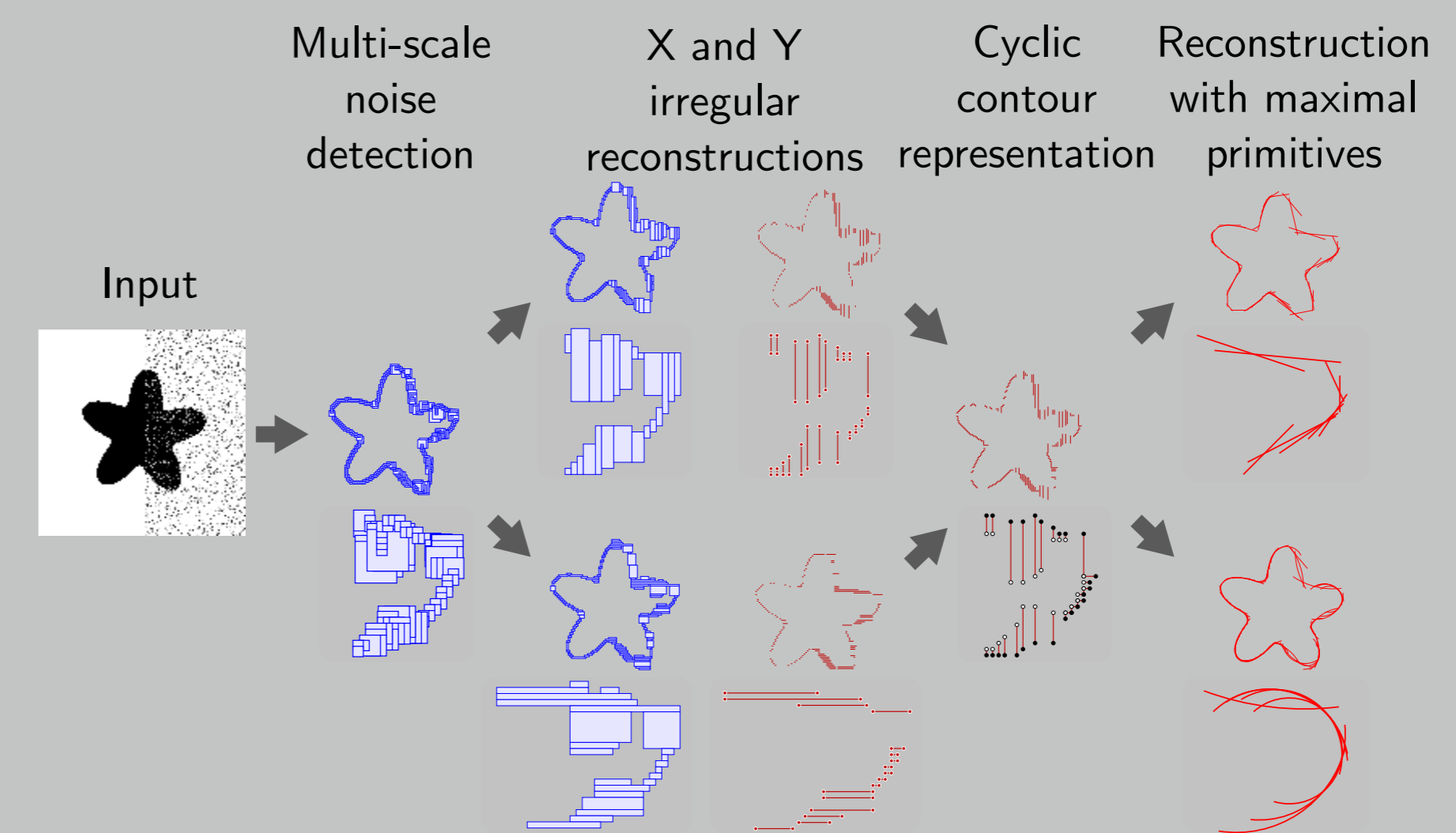
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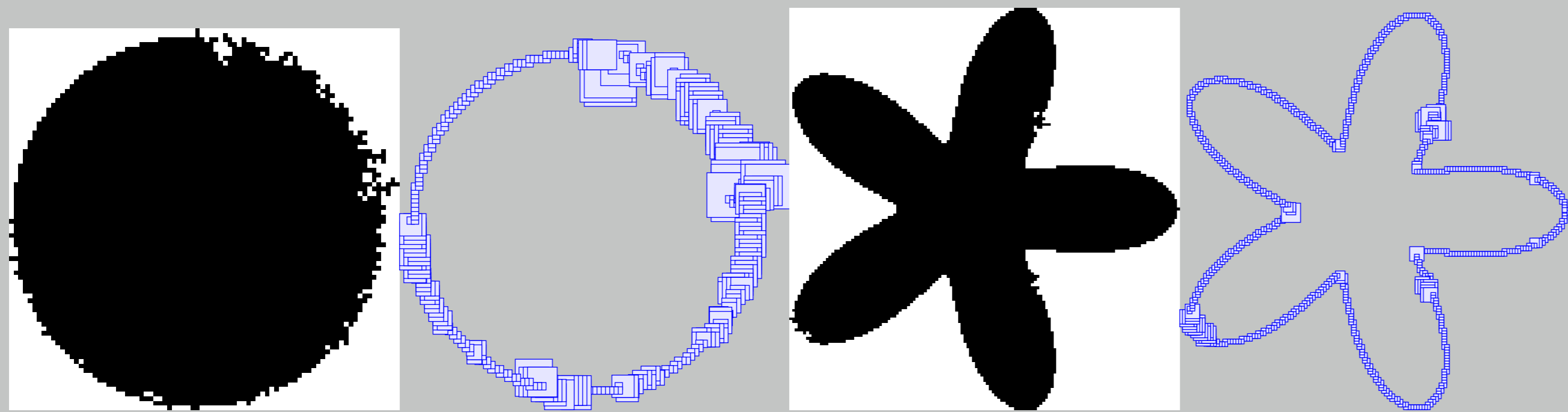
## Overview

- ▶ Our contribution: **novel approach dedicated to noisy contour representations**
- ▶ An extension of [1] enabling calculation of maximal primitives
  - ▷ Straight line segments
  - ▷ Circular arcs
- ▶ Strengths and originalities:
  - ▷ Unsupervised method, without any parameter
  - ▷ 1-D intervals represent the contour, from multi-scale and irregular-grid-based analyses
  - ▷ Generalized linear programming (GLP) calculates maximal primitives from intervals
- ▶ Tested with synthetic and real images



## Multi-scale noise detection

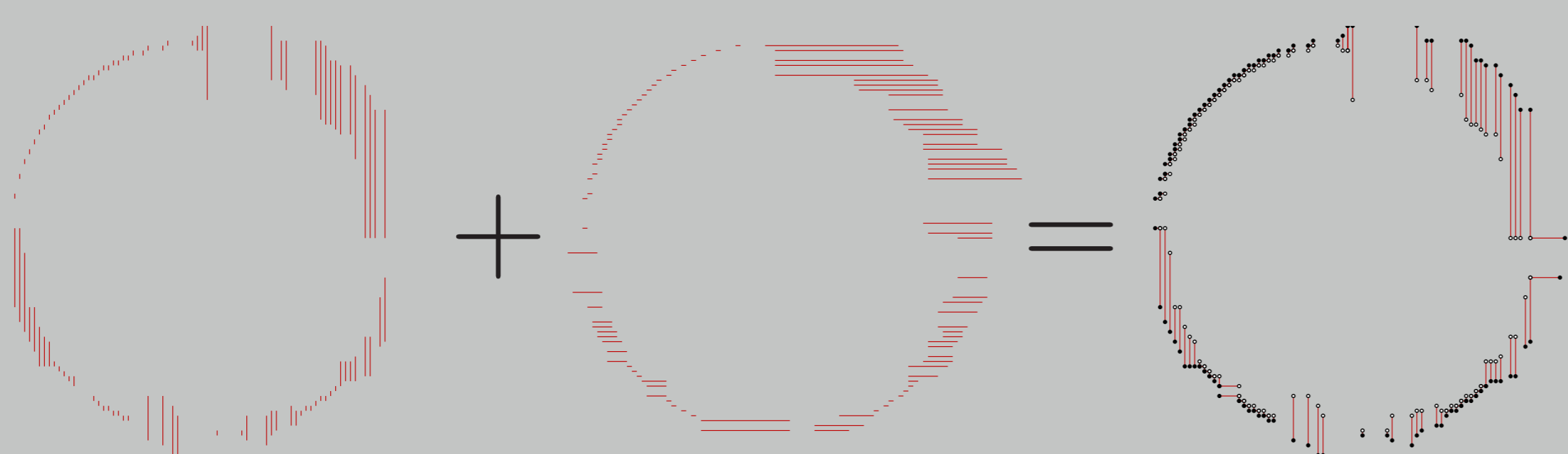
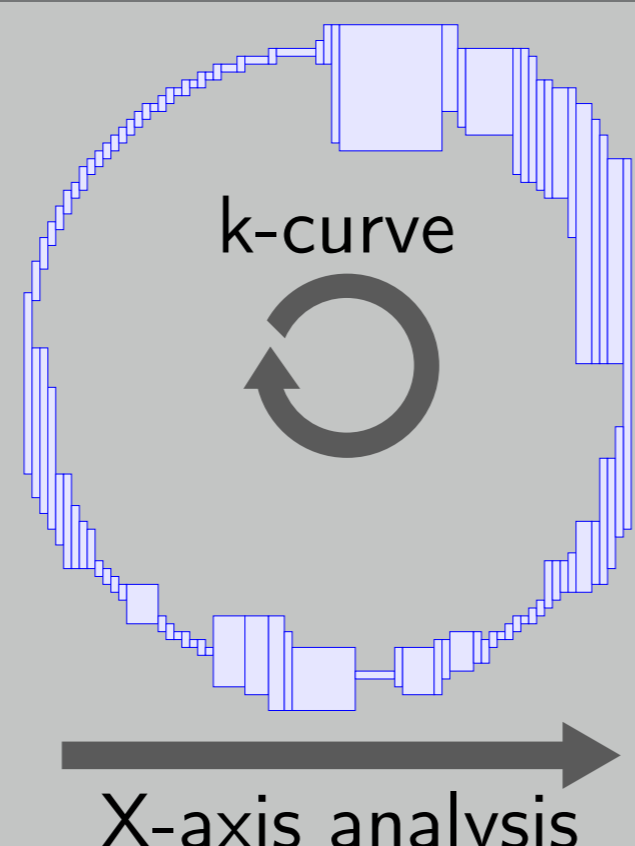
- ▶ Detects automatically the local amount of contour noise [2]
- ▶ Based on multi-scale profile / asymptotic properties of maximal segments
- ▶ Multi-scale output: Large boxes represent large uncertainties



- ▶ **Meaningful boxes** cannot be used directly to reconstruct primitives

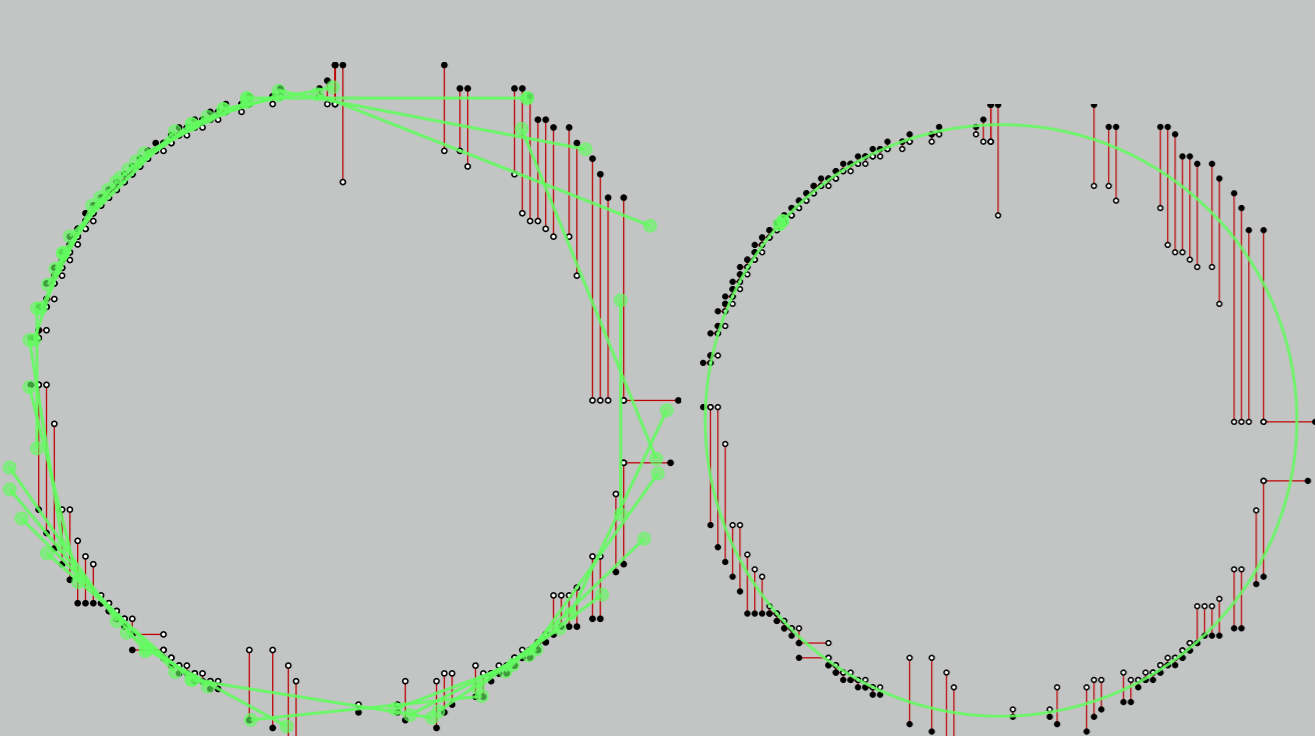
## Irregular isothetic cyclic representation

- ▶ We use irregular isothetic objects
- ▶ Composed of **cells**: adjacent axes-aligned boxes
- ▶ Meaningful boxes analyzed along X and Y axes
- ▶ Reconstructs 2 k-curves (cyclic set of cells)
- ▶ Each k-curve converted into 1-D intervals
- ▶ 2 sets of segments aligned along X- and Y-axes
- ▶ Merged to obtain a single list of 1-D intervals



## Recognition of Straight Segments and Circular Arcs

- ▶ 1-D intervals analyzed by GLP
- ▶ Interval endpoints:
  - ▷ ● black (external) points
  - ▷ ○ white (internal) points
- ▶ **Solving GLP** = finding primitives enclosing ○ and not ●
- ▶ Easy-to-implement, fast and incremental algorithm [3]

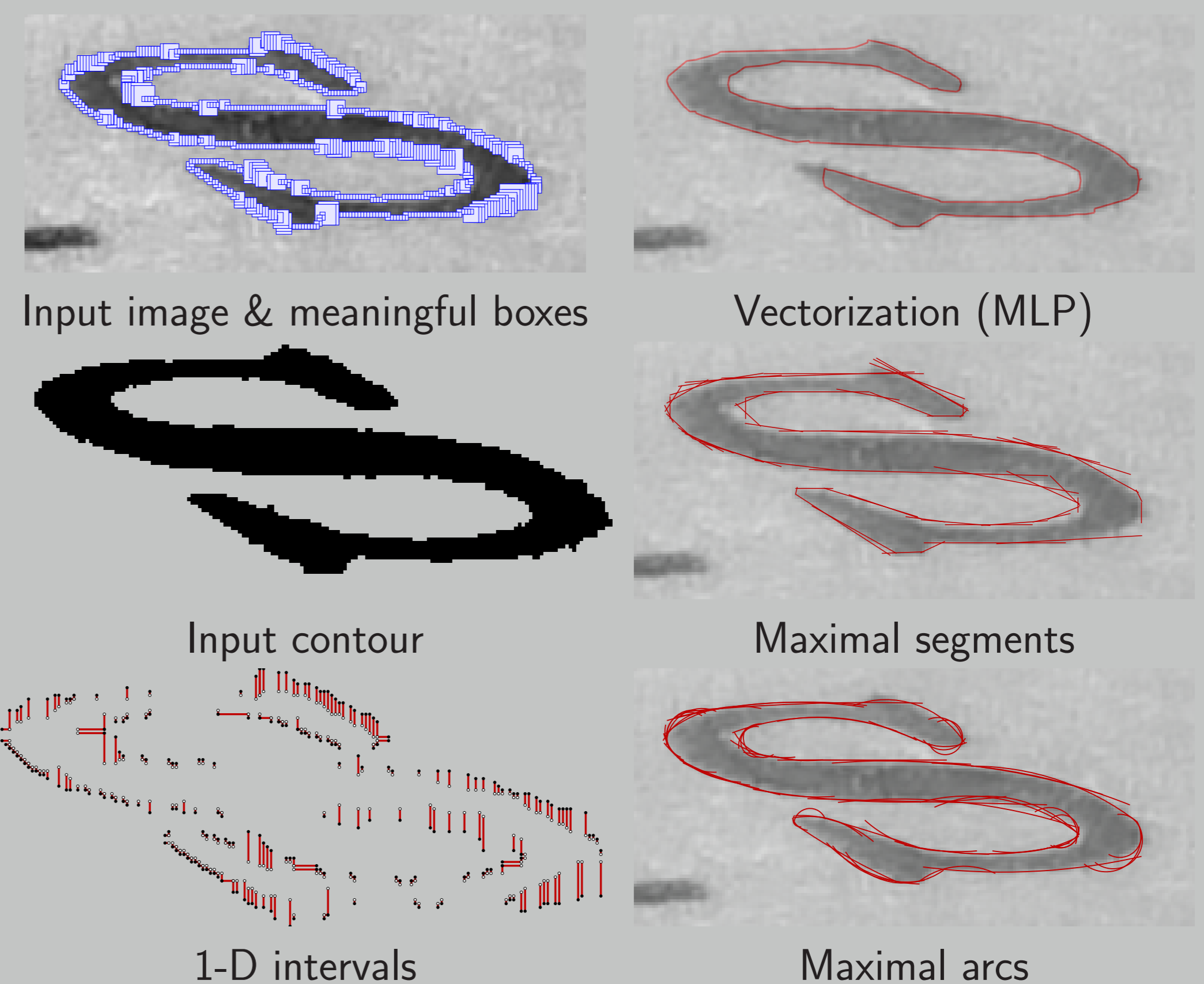


## Experimental results

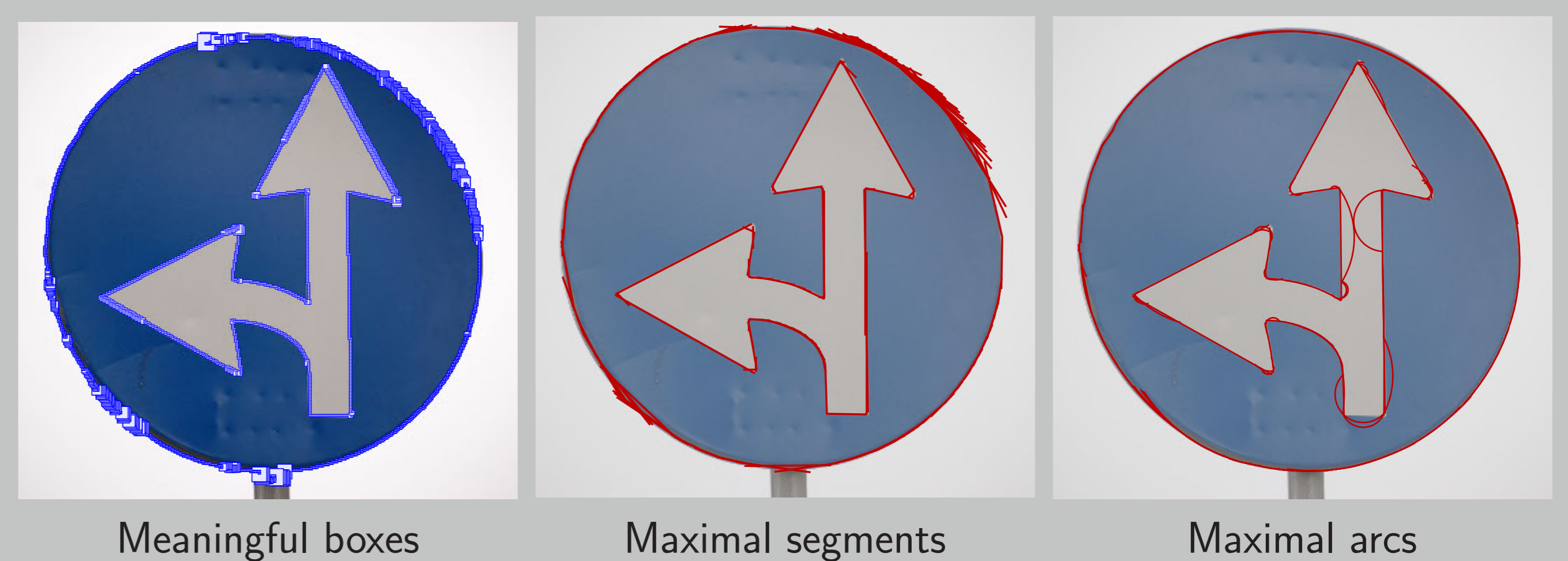


- ▶ I. Maximal segments and arcs with a complex synthetic contour

- ▶ II. Complete pipeline with a scanned character
- ▶ Compared with vectorization by MLP (Minimum Length Polyline)

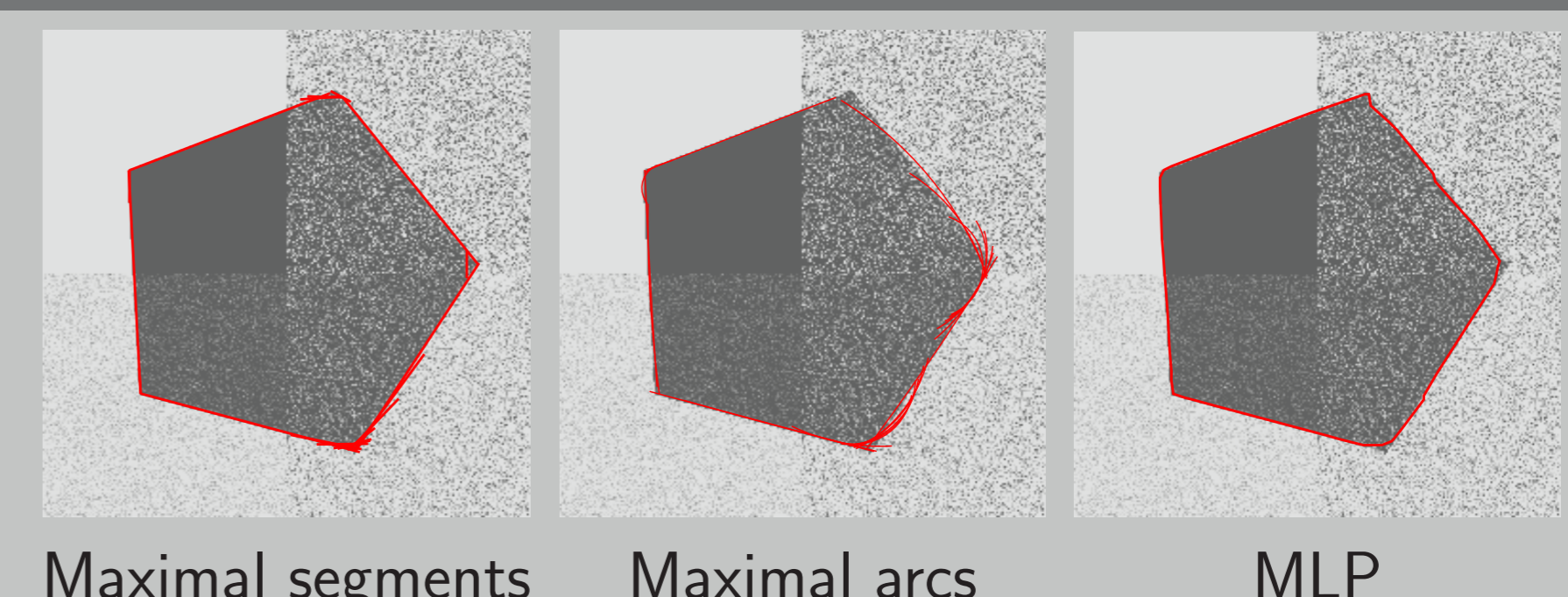


- ▶ III. Final results with a large image with 2 contours
  - ▷ External contour: 1,364 boxes
  - ▷ Internal contour: 1,234 boxes



## Future works

- ▶ Our next step: exploit tangential cover to compute minimal number of primitives [4]
- ▶ Enables the calculation of a single contour representation based on maximal arcs and segments
- ▶ Compare our contribution to other approaches from state-of-the-art
- ▶ Evaluate their robustness with datasets of binary shapes (e.g. KIMIA)
- ▶ How to reconstruct shapes with other geometrical primitives (B-splines, etc.)?



## References

[1] A. Vacavant et al. A Combined Multi-Scale/Irregular Algorithm for the Vectorization of Noisy Digital Contours. *Comp. Vision and Image Und.*, 117(4):438-450, 2013  
 [2] B. Kerautret and J.O. Lachaud. Meaningful Scales Detection along Digital Contours for Unsupervised Local Noise Estimation. *IEEE Transactions on Pattern Anal. and Machine Intel.*, 34(12):2379-2392, 2012  
 [3] M. Sharir and E. Welzl. A Combinatorial Bound for Linear Programming and Related Problems. In *Annual Symp. on Theo. Aspects of Computer Science*, Springer LNCS 577, pp. 567-579, 1992  
 [4] F. Feschet and L. Tougne. On the Min DSS Problem of Closed Discrete Curves. *Disc. App. Math.*, 151(1-3):138-153, 2005