## CSc 30400 Introduction to Theory of Computer Science 2nd Homework Set

1. Figure 1 presents the state diagrams of two DFAs,  $M_1$  and  $M_2$ . Answer the following questions about each of these machines.



Figure 1:  $M_1$  and  $M_2$  of exercise 1.

- (a) What is the start state?
- (b) What is the set of accepting states?
- (c) What sequence of states does the machine go through on input 0011?
- (d) Does the machine accept the string 0011?
- (e) Does the machine accept the string  $\varepsilon$ ?
- 2. The formal definition of a DFA M is  $(\{q_1, q_2, q_3, q_4, q_5\}, \{u,d\}, \delta, q_3, \{q_3\})$ , where  $\delta$  is given by table 1. Give the state diagram of this machine.

	u	d
$q_1$	$q_1$	$q_2$
$q_2$	$q_1$	$q_3$
$q_3$	$q_2$	$q_4$
$q_4$	$q_3$	$q_5$
$q_5$	$q_4$	$q_5$

Table 1: The transition function  $\delta$  of exercise 2.

- 3. Design an automaton on the alphabet  $\Sigma = \{0, 1\}$  that recognizes the language:
  - (a)  $L_1 = \{w | w \text{ contains exactly two } 1s\}$
  - (b)  $L_2 = \{w | w \text{ contains at least two } 1s\}$
  - (c)  $L_3 = \{w | w \text{ contains two consecutive 1s}\}$
  - (d)  $L_4 = \{w | w \text{ contains exactly two 1s and three 0s}\}$
  - (e)  $L_5 = \{w | w \text{ contains an even number of } 1s\}$
  - (f)  $L_6 = \{w | w \text{ contains a number of 1s that is a multiple of 3}\}$
- 4. Imagine a home alarm. This alarm has a numpad with 5 digits (from 1 to 5). The password to deactivate the alarm is set to 3143. Every time that you press a wrong digit you lose a try. Then you should retype the whole password. You have only 3 tries to deactivate the alarm.
  - (a) Design an automaton *Alarm* that describes this alarm. Draw the state diagram. Explain the figure.
  - (b) Determine Q (the set of states), Σ (the alphabet), δ (the transition function), q<sub>0</sub> (the start state) and F (the set of accepting states) in your automaton. What each of the above symbols represent in the alarm? Describe in English.
  - (c) Which is the Language L(Alarm) that this automaton recognizes?
  - (d) How many states does your automaton have? Can you find a minimum equivalent automaton (an automaton with minimum number of states that recognizes the same language)?